
A simple shell model for the break-up of agglomerates in turbulent flows

Yasmine Ammar ^{1;2} and Michael W. Reeks ¹

¹

School of Mechanical and Systems Engineering, Newcastle University, UK ;

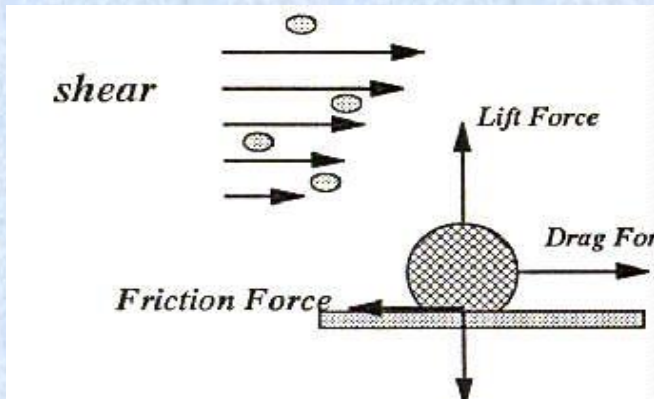
² Thermal-Hydraulics Laboratory, Nuclear Energy and Safety Department, Paul Scherrer Institute, CH-5232, Villigen PSI, Switzerland



Outline

- Escape of particles from potential wells
 - Role of the turbulence
 - Removal rate
 - Rock n roll model
- Characterising agglomerates
- Shell model for breakup
- Prediction versus experimental results
 - ARTIST experiment

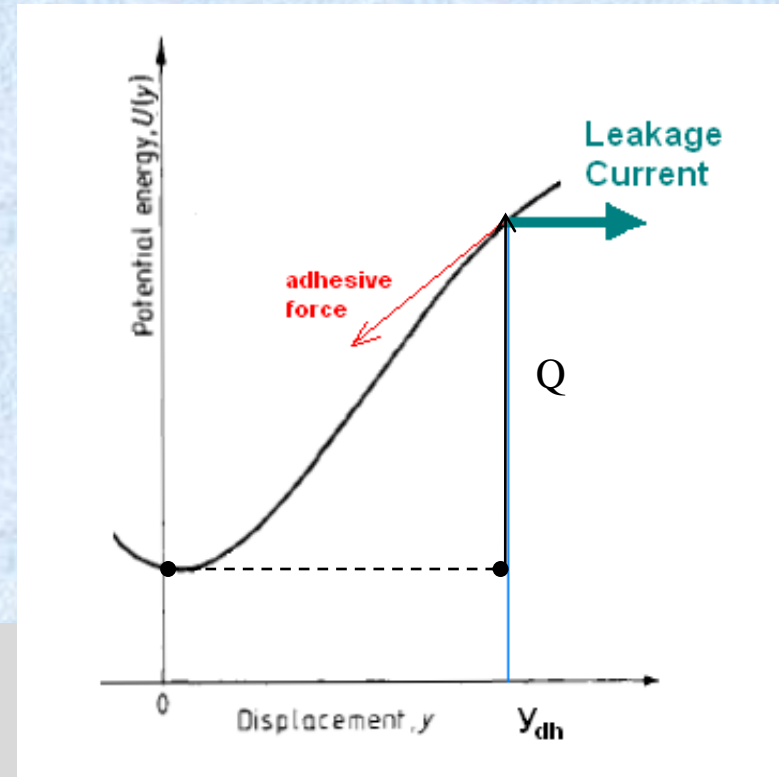
Escape of particles from potential wells



particle resuspension

$$p = \omega \exp - Q / 2 \langle PE \rangle$$

- p , the resuspension rate constant
- ω , the typical frequency of vibration,
- Q height of adhesive potential well,
- $\langle PE \rangle$ average potential energy of particle in the well.



Particle escape from potential well

Rock'n'Roll Model (Reeks & Hall, 2001)

Fraction remaining after 1 sec

and resuspension rate:

$$f_R(t) = \int_0^\infty e^{-p(f'_a)t} \varphi(f'_a) df'_a$$

$$\Lambda(t) = \int_0^\infty p(f'_a) e^{-p(f'_a)t} \varphi(f'_a) df'_a$$

$$p = \frac{\omega_0}{2\pi} \exp\left(-\frac{k(f_a - \langle F \rangle)^2}{\langle f^2 \rangle (1 + \eta)}\right)$$

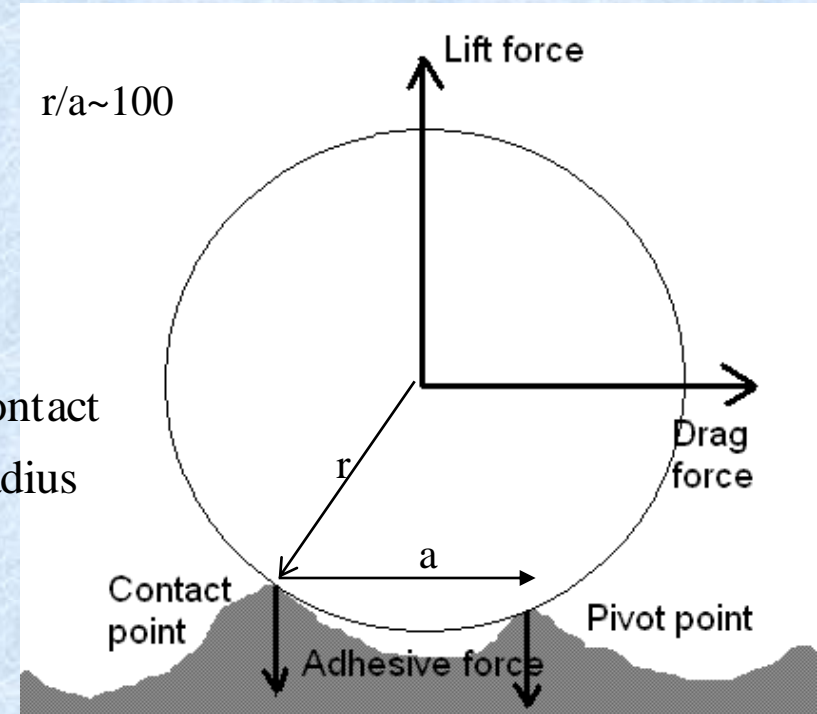
f_a = adhesive force F_a = adhesive for perfect contact

$F_a = 3\pi\gamma r$, γ = surface energy, r = particle radius

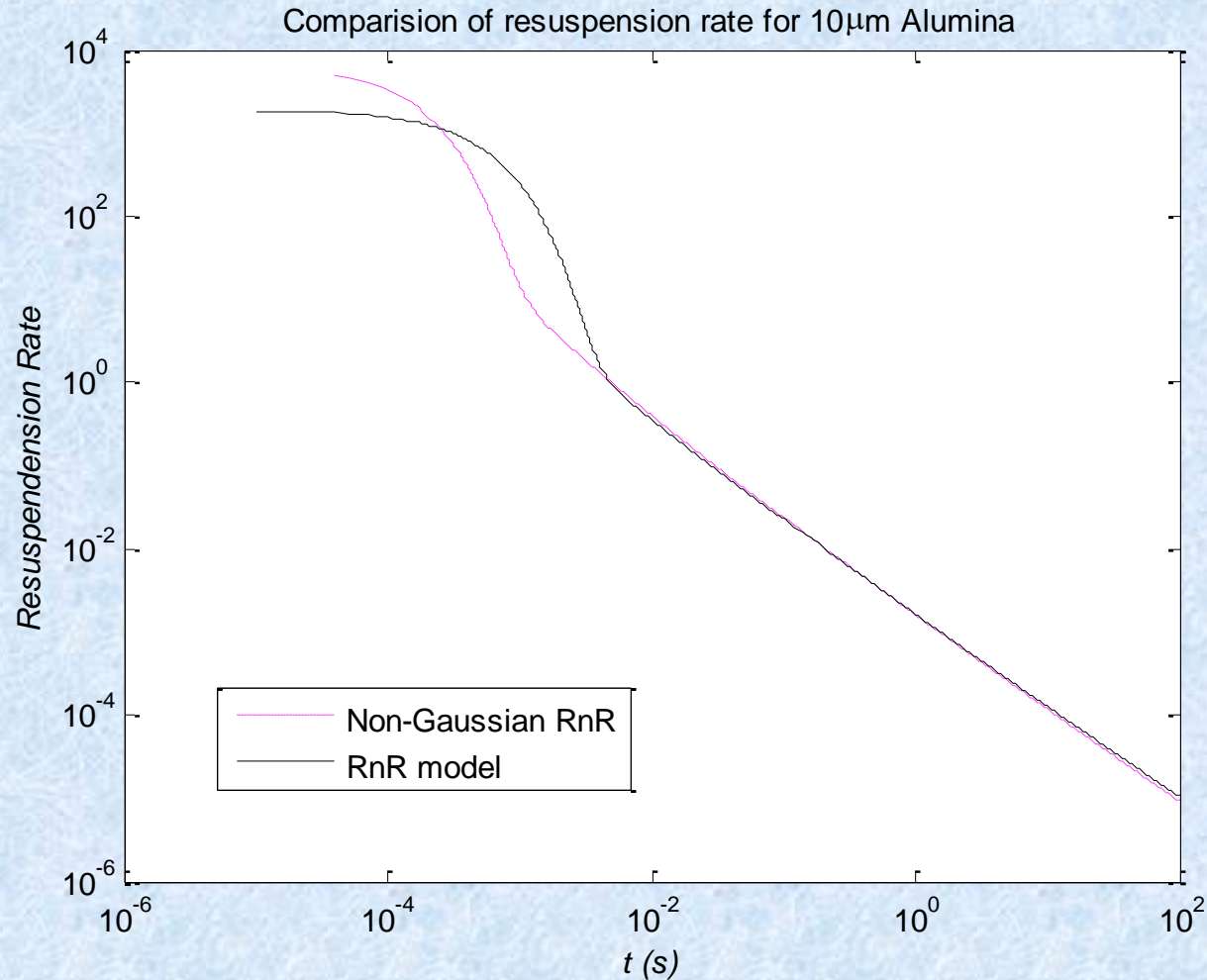
$f'_a = f_a / F_a$; $\varphi(f'_a)$ Lognormal distribution

Biasi *et al.* (2001) $\langle f'_a \rangle = 0.016 - 0.0023r^{0.545}$

$\sigma'_a = 1.8 + 0.136r^{1.4}$, r in microns



Short and long term removal rates



Mechanism for Agglomerate breakup

- Rupture
 - Break-up into fragments -daughter agglomerates
 - similar to particle removal from a surface
 - Threshold for aerodynamic forces based on strength of agglomerate
 - Continues until agglomerates reaches a minimum size
 - Usually 3 or 4 daughter fragments
- Erosion
 - Lower aerodynamic forces than rupture
 - Much slower than breakup due to rupture
 - Onion peeling mechanism
 - Use of kinetic / stochastic models

Characterising an Agglomerate

For a fractal agglomerate, the number of primary particles within the agglomerate is given by:

$$N_p = k_o \left(R_c / r_p \right)^{d_f}$$

$k_o \approx 0.42d_f - 0.22$ in the range $1.50 \leq d_f \leq 2.75$

d_f is the fractal dimension.

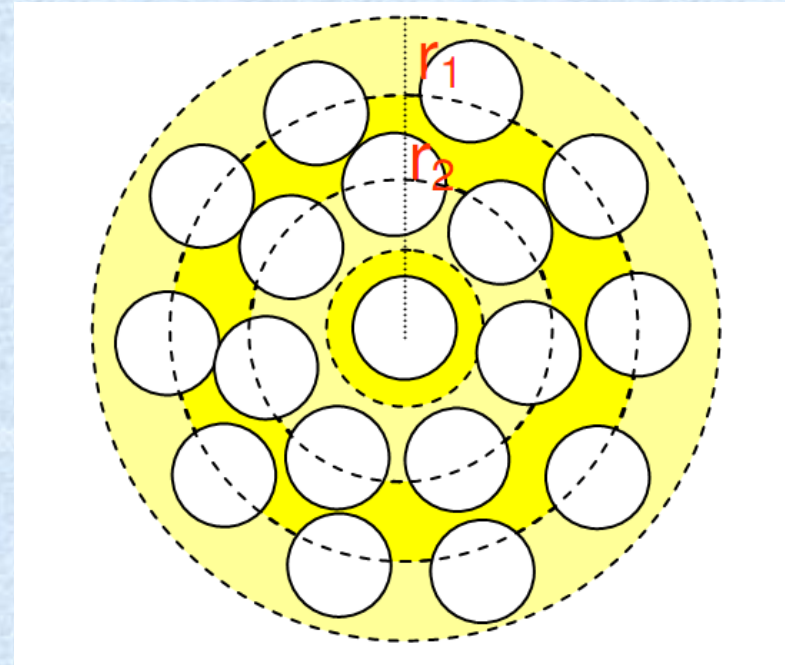
R_c is the collision or outer radius

r_p is the primary particle radius

volume fraction of the particle

$$\phi = \frac{V_m}{V_p}$$

V_m is the material volume
 V_p is the volume of the particle
the material and void volume



$$\phi(r) = k_o \frac{d_f}{3} \left(\frac{r}{r_p} \right)^{d_f - 3}$$

Characterising agglomerate

The average thickness of the l -th shell $\overline{\Delta r_l}$ will depend upon the volume fraction and the distribution of particles sizes within each shell. It is given by

$$\overline{\Delta r_l} = \left(\frac{v_p}{\phi(R_{l+1})} \right)^{1/3}$$

The l -th shell outer radius is then defined as:

$$R_l = r_p + \sum_{i=1}^l \overline{\Delta r_i}$$

And the radius of the l -th shell which is half way between the outer and inner radii of the shell is then:

$$r_l = \frac{1}{2}(R_l + R_{l+1})$$

The number of particles in the k -th shell is given by:

$$\overline{n_{pl}} = N_p(r_{l+1}) - N_p(r_l)$$

Equations for the breakup rate

$p(\xi)$ is the rate constant for removal of particles from an adhesive potential well characterised by ξ

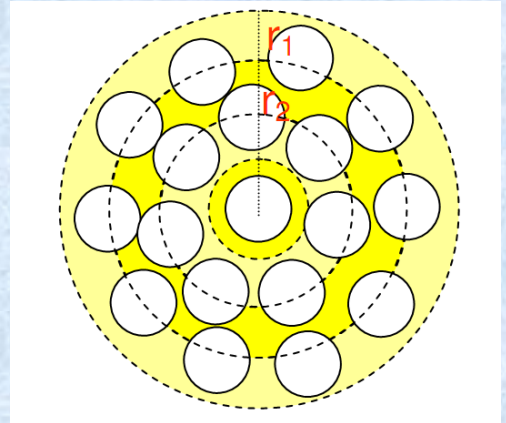
The total removal rate of particles being an integration over a broad range of adhesive potential, i.e. values of ξ due to a distribution of particle sizes, microscale roughness and flow exposure

The removal rate of particles from any given shell/layer depends upon the rate at which particles are exposed to the flow by removal of particles from the shell above

If $n_i(\xi, t)$ is the number of particles in the layer i with adhesive and flow parameters between $\xi, \xi+d\xi$, with pdf $\psi(\xi)$

$$\begin{aligned} \frac{\partial n_i(\xi, t)}{\partial t} &= -p(\xi)n_i(\xi, t) + \psi(\xi) \int_0^\infty p(\xi')n_{i-1}(\xi', t)d\xi' \\ &= -p(\xi)n_i(\xi, t) + \psi(\xi)\Lambda_{i-1}(t) \end{aligned}$$

coverage coefficient =1



rms fluctuating drag force

RMS flow velocities in the radial (longitudinal) and azimuthal (lateral) directions for

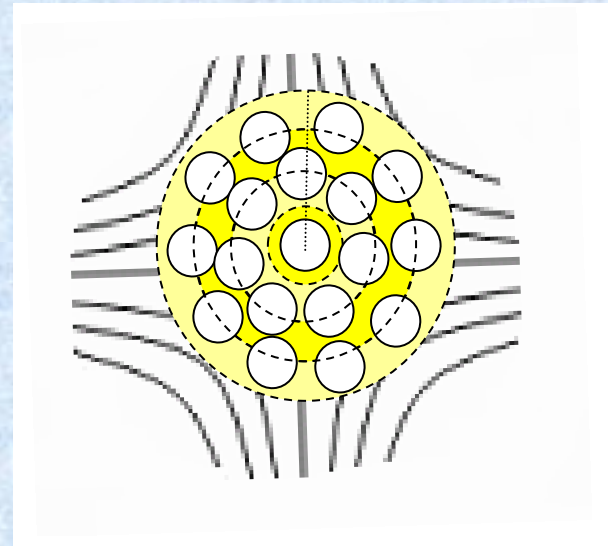
$$\sqrt{v_r^2} = \sqrt{v_\theta^2} = \left(\overline{\dot{\gamma}^2}\right)^{1/2} r / \sqrt{2}$$

rms radial drag force

$$\sigma^2 = \frac{1}{2} \overline{\dot{\gamma}^2} \beta_\tau^2 r^2,$$

The adhesive force f_a is selected from a lognormal distribution

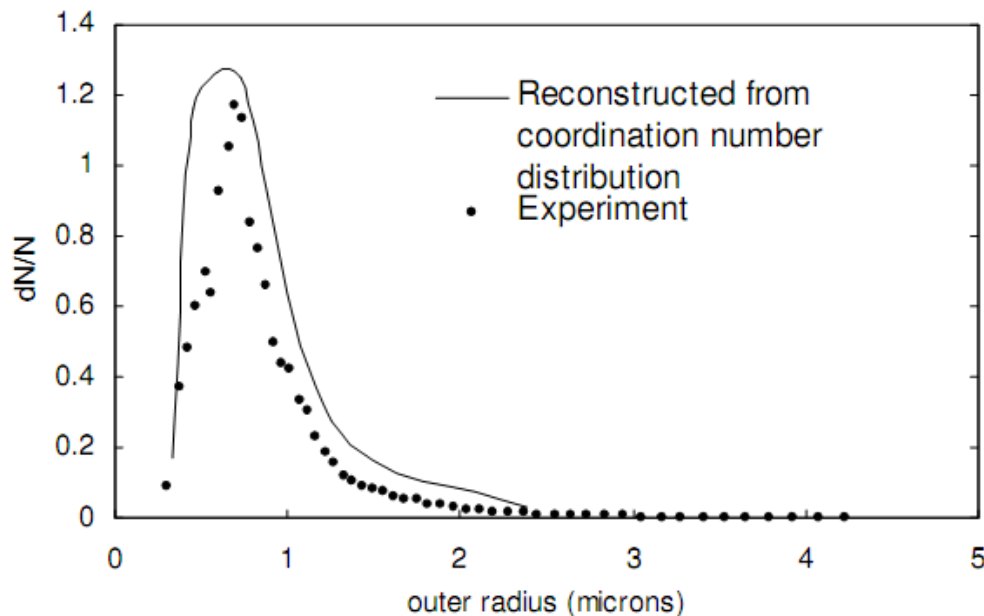
$$\varphi(f_a') = \frac{1}{\sqrt{2\pi}} \left(\frac{1}{f_a' \ln \sigma_a'} \right) \exp \left(-\frac{1}{2} \left[\frac{\ln(f_a' / \overline{f_a'})}{\ln \sigma_a'} \right]^2 \right)$$



f_a' is normalized by the Van der Waals force F_a between 2 spheres in perfectly smooth contact, which is, according to Equation (2.53), $F_a = \frac{3}{2} \pi \Gamma_a r_a$ and reduced by a factor of the order 100 due to the roughness of the contact

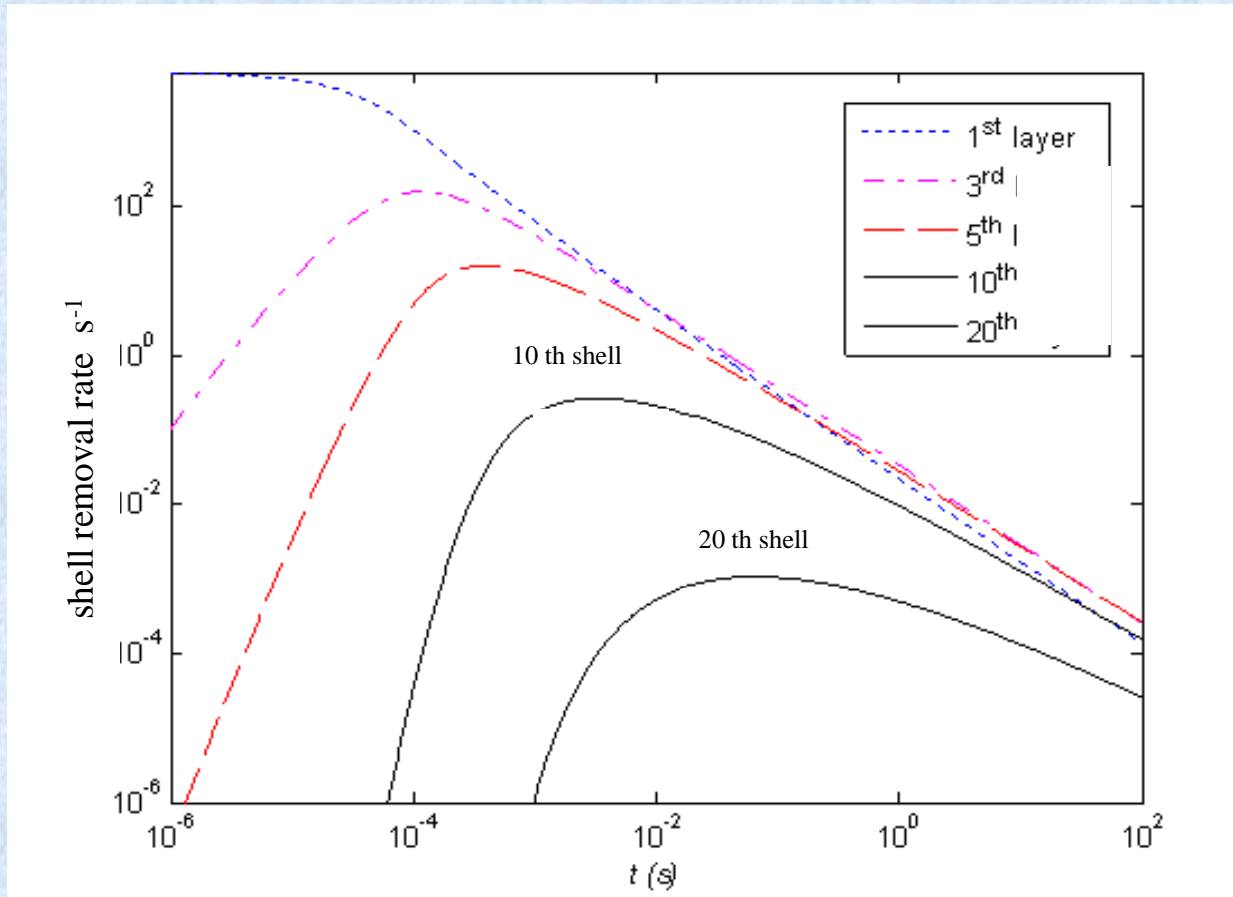
Distribution of clusters within agglomerate

Figure 8.3: Fragment Size distribution obtained experimentally compared to the reconstructed fragment size distribution based on the coordination distribution

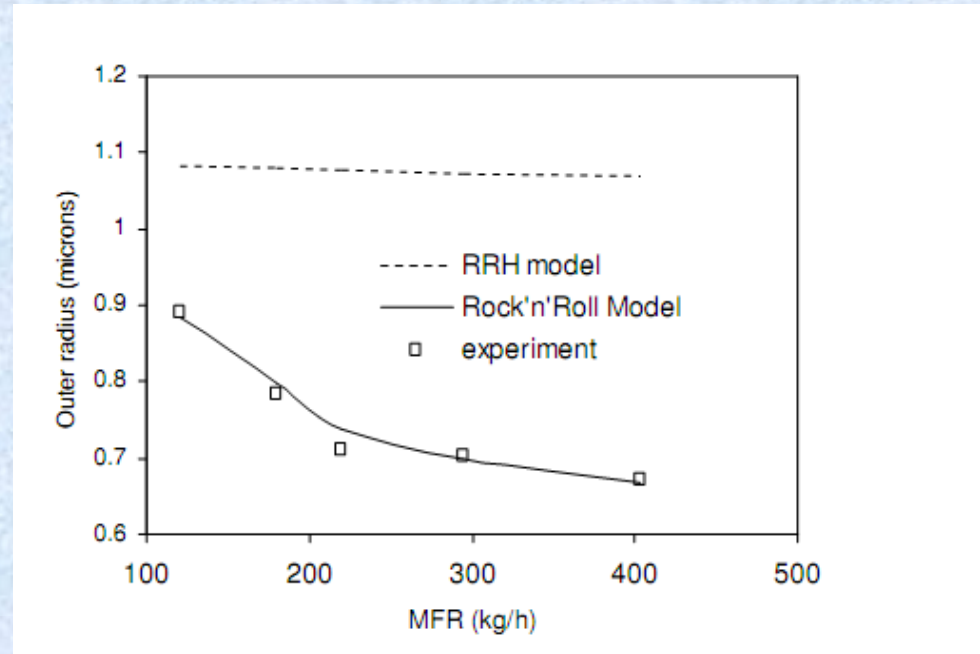
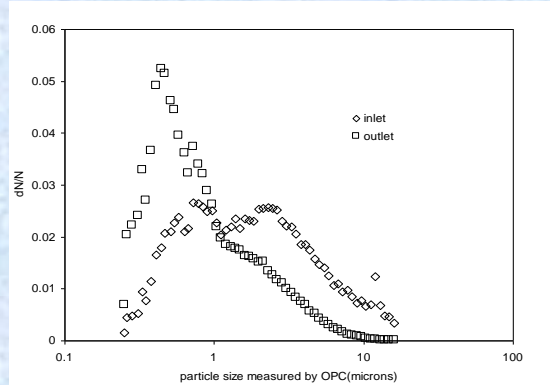


Agglomerates are fragments 48% triplets, 22% quartets, 25% quintets, ..

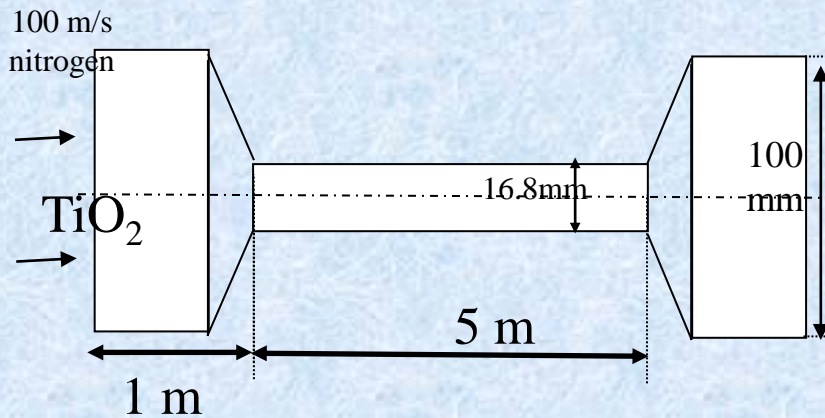
Shell removal rates



experimental results and model predictions



reduction factor of the adhesive forces ~500.
 (r/a) is ~ 100
 spread of the adhesive forces ~10



Summary & conclusions

- Model for agglomerate break up
 - Analogous to removal of a particles from surfaces in turbulent boundary layers
 - Escape of particles from adhesive potential wells
 - Motion driven by fluctuating aerodynamic forces/ moments
 - Rock and roll about surface asperities
 - Shell model similar to multilayer resuspension
 - removal particles from any shell/leer rate limited by removal of particles from the layer above
 - Future developments
 - DNS of flows within agglomerates
 - Calculation of forces on individual primary particles
-