



Predicting pressure drop in a pipe flow of concentrated pulp suspensions

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 **cost**
EUROPEAN COOPERATION
IN SCIENCE AND TECHNOLOGY



- Objectives
- Experimental data
- Previous studies
- Numerical model
- Bartosik damping function
- Numerical results
- Conclusions & Future work



Modelling the flow of concentrated fiber suspensions in pipes
using commercial CFD code

"Using CFD to model fibre suspensions flows - FIBERFLOW"

- **Characterization of the pulp suspension rheology**
- **Adaption of low-Reynolds (LRN) $k-\varepsilon$ turbulence models** to take into account the presence of fibers – **source terms** and **rheological model**
- **Validation of the model**



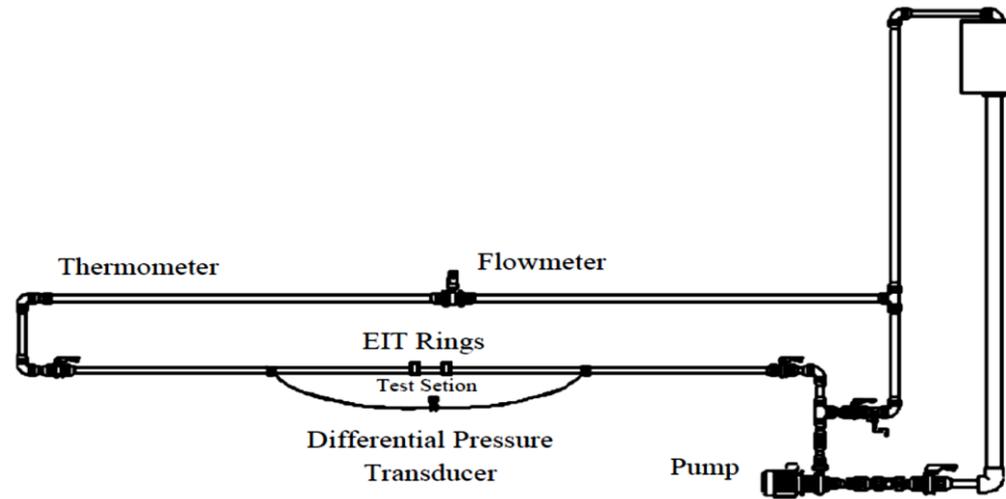
Experimental data - Pressure drop

Eucalyptus pulp suspension

- Fiber length = 0.706 mm
- $D_{fiber} = 16\mu\text{m}$
- $\rho = 998.2 \text{ kg/m}^3$

- **test section:** D=7.62cm L=4m
- **Main result:** pressure drop

c [% w/w]	N Crowding factor	Case	U_{bulk} [m·s ⁻¹]	$\Delta P/L_{exp.}$ [Pa·m ⁻¹]
1.50	1947	A	4.49	829
		B	6.21	1289
2.50	3245	C	4.90	2299
		D	5.55	2814



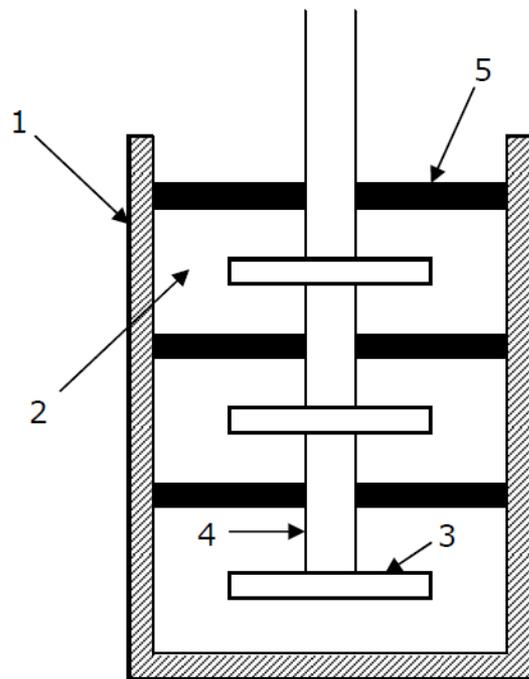
Schematic view of the pilot rig (adapted from Ventura *et al* 2008)

Crowding factor

$$N = \frac{2}{3} c_v \left(\frac{L_{fiber}}{D_{fiber}} \right)^2$$

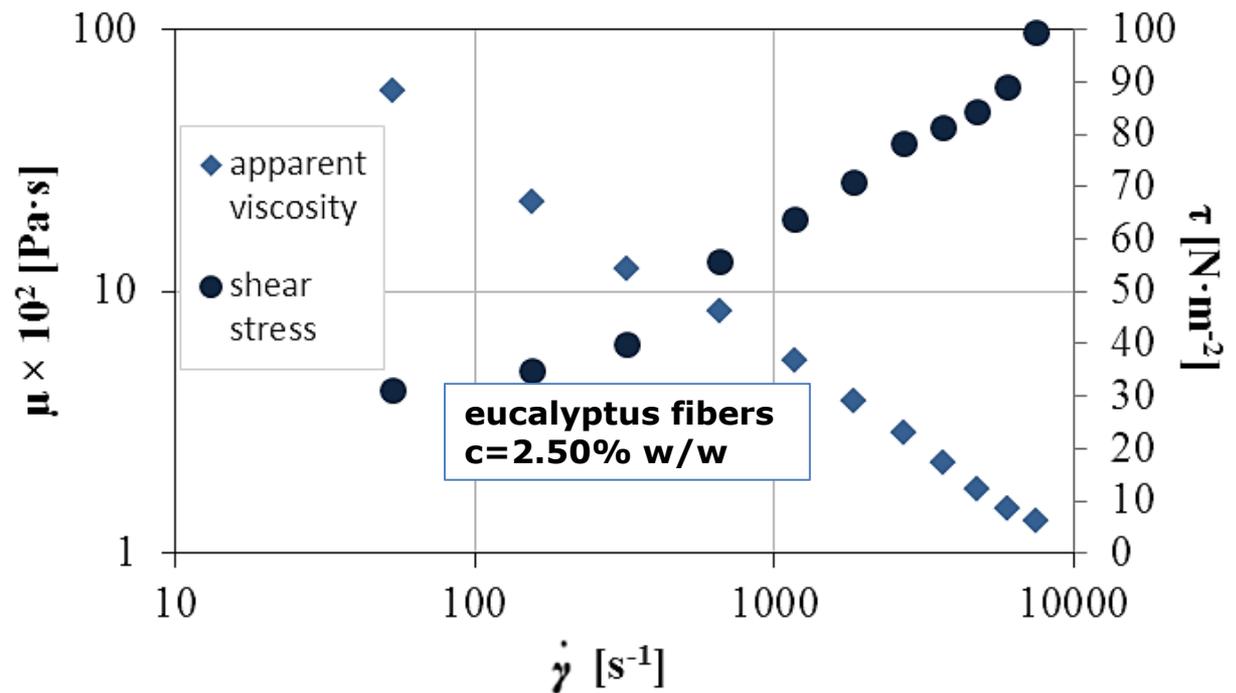
Ventura, C.; Garcia, F.; Ferreira, P.; Rasteiro, M. (2008) – "Flow Dynamics of Pulp Fiber suspensions" – TAPPI Journal, 7(8): 20-26

Searle-type Plate viscometer
Blanco *et al* (2007)



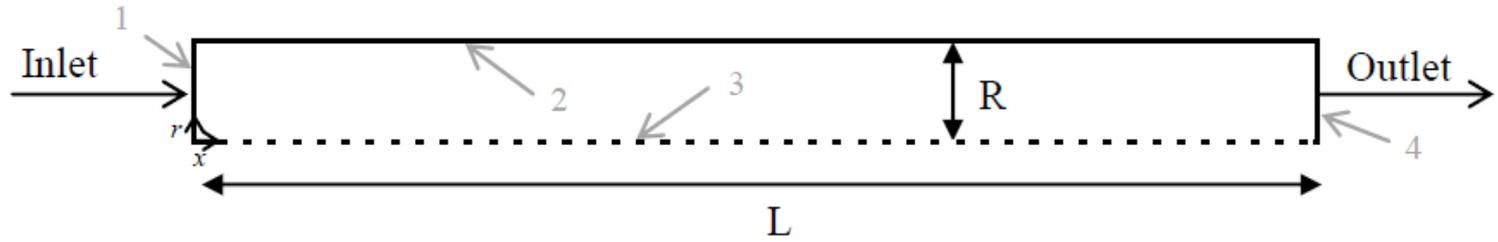
- 1 - Vessel
- 2 - Sample
- 3 - Moving plates
- 4 - Rotor
- 5 - Fixed plates

Output data:
 τ - shear stress (torque)
 $\dot{\gamma}$ - shear rate (rotational speed)





Numerical model



$R = 0.0381 \text{ m}$
 $L = 1 \text{ m}$

Location	Left Side 1	Right Side 4	Bottom 3	Top 2
Boundary Condition	Periodic boundaries		Axis	Wall

- *single-phase (continuum)*
- *steady state (fully developed flow)*
- *isothermal*
- *incompressible*
- *2D axisymmetrical flow*
- *non-Newtonian fluid viscosity*
- *water annulus - water viscosity*



General transport equation

$$\frac{1}{r} \left[\frac{\partial}{\partial x} (r\rho u\phi) + \frac{\partial}{\partial r} (r\rho v\phi) \right] = \frac{1}{r} \left[\frac{\partial}{\partial x} \left(r\Gamma_\phi \frac{\partial\phi}{\partial x} \right) + \frac{\partial}{\partial r} \left(r\Gamma_\phi \frac{\partial\phi}{\partial r} \right) \right] + S_\phi$$

dependent variables ϕ , diffusibility term Γ_ϕ and source-term S_ϕ (Hsieh and Chang, 1996).

Equation	ϕ	Γ_ϕ	S_ϕ
Continuity	1	0	0
Momentum - axial	u	$\mu_{eff} = \mu + \mu_t$	$-\frac{\partial P}{\partial x} + \frac{\partial}{\partial x} \left(\mu_{eff} \frac{\partial u}{\partial x} \right) + \frac{1}{r} \frac{\partial}{\partial r} \left(r\mu_{eff} \frac{\partial v}{\partial r} \right)$
Momentum - radial	v	$\mu_{eff} = \mu + \mu_t$	$-\frac{\partial P}{\partial r} + \frac{\partial}{\partial x} \left(\mu_{eff} \frac{\partial u}{\partial r} \right) + \frac{1}{r} \frac{\partial}{\partial r} \left(r\mu_{eff} \frac{\partial v}{\partial r} \right) - 2\mu_{eff} \frac{v}{r^2}$
Kinetic energy	k	$\mu + \mu_t / \sigma_k$	$G_k - \rho\varepsilon$
Dissipation rate	ε	$\mu + \mu_t / \sigma_\varepsilon$	$(C_{\varepsilon 1} f_1 G_k - C_{\varepsilon 2} f_2 \rho\varepsilon) \varepsilon / k$

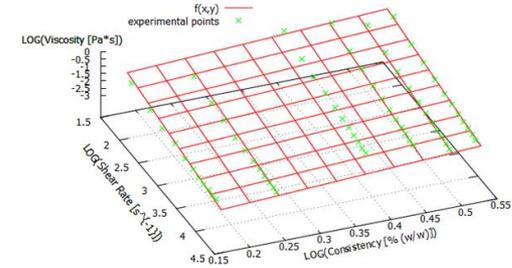
$$G_k = \mu_t \left\{ 2 \left[\left(\frac{\partial u}{\partial x} \right)^2 + \left(\frac{\partial v}{\partial r} \right)^2 + \left(\frac{v}{r} \right)^2 \right] + \left(\frac{\partial v}{\partial x} + \frac{\partial u}{\partial r} \right)^2 \right\}; \quad \mu_t = \rho C_\mu f_\mu k^2 / \varepsilon$$



- **6 built-in LRN turbulence models were evaluated**
- **2 different rheological models were evaluated:**

$$\eta_{app} = K \left(\dot{\gamma} \right)^n \quad (n < 0)$$

$$\eta_{app} = \frac{c a_1}{a_0 \dot{\gamma}} \cdot a_2$$



- A **drag reduction** can be observed in **all cases** when using **LRN turbulence models**
- The models of **Abe-Kondoh-Nagano (AKN)** and **Chang-Hsieh-Chen (CHC)** showed the best fit to the experimental data
- The **damping function f_μ** can be **modified** taking into account the literature for **polymer solutions flows (Malin damping function)** and for **particle suspensions flow (Bartosik damping function)**.
- The application of the **damping function of Malin** was not able to improve the numerical results.
- The numerical results **can be improved significantly** by applying an **“optimized” Malin damping function**.
- **Further improvement needed...**



The best fit of experimental rheological data modified expression

pulp consistencies c [%]:
1.50, 1.80, 2.50
2.90, 3.20, 3.50

$$\eta_{app} = \frac{c^{a1}}{a0} \cdot 10^{a2}$$

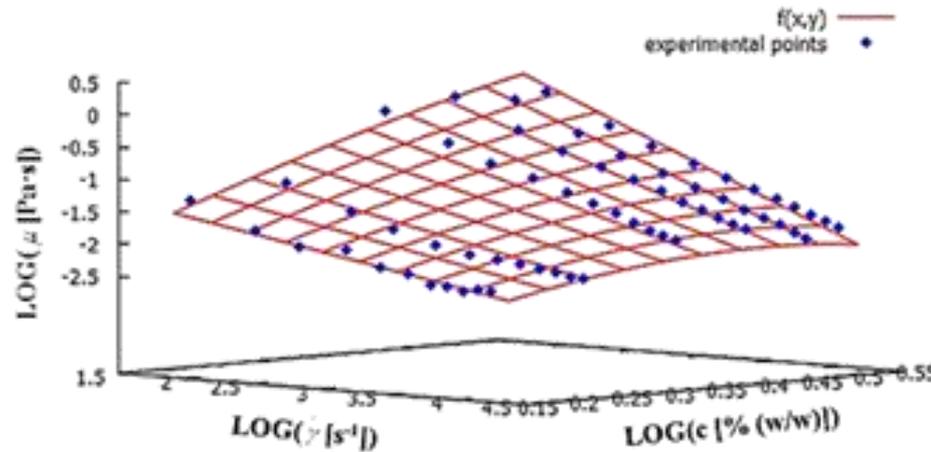
$$\eta_{app} = \frac{c^{a1}}{a0 \cdot c} \cdot 10^{a2}$$

$a0=0.683566$
 $a1=2.39972$
 $a2=-0.225815$

$a0=0.259433$
 $a1=6.97456$
 $a2=-2.07198$

$R^2=0.954$

$R^2=0.984$





- **Modification** of the **damping functions** f_μ of the **AKN** and **CHC** turbulence models (implemented in Ansys Fluent) according to **Bartosik (2011)** for **particle suspensions flow** (uniform particles distribution):

$$f_\mu = 0.09 \exp \left[- \frac{-3.4 [1 + A_s^3 d^2 (8 - 88 A_s d) c_v^{0.5}]}{\left(1 + \frac{Re_t}{50}\right)^2} \right]$$

A_s - empirical constant (=100)
 c_v - averaged volume fraction of solids
 d - averaged solid particles diameter

- Modification the constants of the Bartosik damping function:

$$f_\mu = \boxed{C} \cdot \exp \left[- \frac{-3.4 [1 + \boxed{A}^3 \boxed{B}^2 (8 - 88 \cdot \boxed{A} \cdot \boxed{B}) c_v^{0.5}]}{\left(1 + \frac{Re_t}{50}\right)^2} \right]$$

$$Re_T = \frac{k^2}{\epsilon \nu}$$

Bartosik, A. - "Mathematical modelling of slurry flow with medium solid particles" - Mathematical Models and Methods in Modern Science, International Conference Mathematical Models and Methods in Modern Science, Spain, 10-12 December, 2011. ISBN 978-1-6-61804-055-8, pp.124-129.



Simulation results

Convergence criterion = 1×10^{-5}
 Water annulus and non-Newtonian fluid

$$\eta_{app} = \frac{c^{a1}}{a0 \cdot c} \cdot 10^{a2} \cdot \gamma$$

c [% w/w]	U_{in} [m·s ⁻¹]	$\Delta P/L_{exp.}$ [Pa·m ⁻¹]	$\Delta P/L_{num}$ [Pa·m ⁻¹]	δ [%]						
1.50	4.49	829	1560	88	1032	24	1763	113	1022	23
	6.21	1289	387	70	1776	38	3164	146	2026	57
2.50	4.90	2299	1861	18	1624	3	1843	17	1632	3
	5.55	2814	2046	17	1800	3	2022	16	1811	3
				AKN	AKN-Bartosik		CHC		CHC-Bartosik	



- A *drag reduction* can be observed in all cases when **AKN** and **CHC** turbulence models are used.
- Results allow to conclude that the **AKN** and **CHC** models modified with the **damping function of Bartosik** show a **better fit** to the experimental data.
- To improve the numerical results, the constants of **Bartosik damping function** f_μ can be **modified** - A_s and d for the pulp flow can be different from those used by Bartosik to study the **particle** suspensions flow.



Bartosik damping function

$$f_{\mu} = C \cdot \exp \left[- \frac{-3.4 [1 + A^3 B^2 (8 - 88 \cdot A \cdot B) c_v^{0.5}]}{\left(1 + \frac{Re_t}{50}\right)^2} \right]$$

	Case							
	1	2	3	4	5	6	7	8
A	100	50	150	100	100	100	100	100
B × 10⁵	1.6	1.6	1.6	70.6	1.6	1.6	1.6	1.6
C × 10²	9	9	9	9	6.75	4.75	3.75	2.45

- Change of **A** does not have a significant effect on the numerical pressure drop
- Change of **B** (regarded as fiber length instead of the fiber diameter) does not influence significantly the numerical pressure drop



New damping function tested – Bartosik (**AKN** model modified)

Case	Modification	c [% w/w]	U_b [m·s ⁻¹]	Re_w	$\Delta P/L_{exp.}$ [Pa·m ⁻¹]	$\Delta P/L_{num.}$ [Pa·m ⁻¹]	δ [%]
A1	AKN-Bartosik	1.50	4.49	62830	829	1032	24
B1		1.50	6.21	95822	1289	1776	38
C1		2.50	4.90	15904	1579	1624	3
D1		2.50	5.55	19479	1754	1800	3
A6	C=0.0475	1.50	4.49	63071	829	808	3
B7	C=0.0375	1.50	6.21	96694	1289	1298	1
C5	C=0.0675	2.50	4.90	15868	1579	1577	0.1
D5	C=0.0675	2.50	5.55	19467	1754	1750	0.2



New damping function tested – Bartosik (AKN model modified)

- The **AKN** LRN turbulence model considering the **Bartosik damping function f_μ** with **C modified** improves the numerical results.

- The parameter **C** should be **lower** than the value used by Bartosik for particle suspensions flow.

0.09 -> 0.04-0.07



New damping function tested – Bartosik (**CHC** model modified)

Case	Modification	c [% w/w]	U_b [m·s ⁻¹]	Re_w	$\Delta P/L_{exp.}$ [Pa·m ⁻¹]	$\Delta P/L_{num.}$ [Pa·m ⁻¹]	δ [%]
A1	CHC-Bartosik	1.50	4.49	62531	829	1022	23
B1		1.50	6.21	94868	1289	2026	57
C1		2.50	4.90	16357	1579	1632	3
D1		2.50	5.55	20040	1754	1811	3
A6	C=0.0475	1.50	4.49	62403	829	832	0.3
B8	C=0.0245	1.50	6.21	95583	1289	1302	1
C5	C=0.0675	2.50	4.90	16270	1579	1587	0.5
D5	C=0.0675	2.50	5.55	20009	1754	1761	0.4



New damping function tested – Bartosik (CHC model modified)

- The numerical pressure drop, U^+ and k profiles are very similar to that obtained with the AKN-Bartosik model modified ($c=2.50\%$ (w/w))
- The **CHC** LRN turbulence model considering the **Bartosik damping function f_μ** with **C modified** improves significantly the numerical results
- The parameter **C** should be **lower** than the value used by Bartosik for particle suspensions flow, mainly, for $c=1.50\%$ (w/w)

0.09 -> 0.025-0.07



- The **non-Newtonian behaviour of pulp** can be expressed as a function of **shear rate** and **pulp consistency** - a **power-law** considering the **consistency index** and the **flow behaviour** index as a function of **pulp consistency**
- The **damping function f_μ** on these models **can be modified taking into account** the cases from literature for the simulation of **particles turbulent flow**
- **Modifications of** the AKN and CHC LRN turbulence models with the damping function according to **Bartosik** lead to **better fit** to the experimental data
- **Noticeable improvement** of the numerical results can be obtained by **modifying the Bartosik damping function**
- **Model should be used with care - limited applicability**
- **Prediction of pressure drop in a pipe flow of pulp suspensions is a challenging task -> need of further studies...**



- Simulation of wider range of fibre consistencies - to generalize the model
- Study the modification of the damping function f_μ according to Bartosik (2010):

$$f_\mu = 0.09 \exp \left[\frac{-3.4 \left(1 + \frac{\tau_0}{\tau_w} \right)}{\left(1 + \frac{Re_t}{50} \right)^2} \right]$$

τ_0 - yield stress

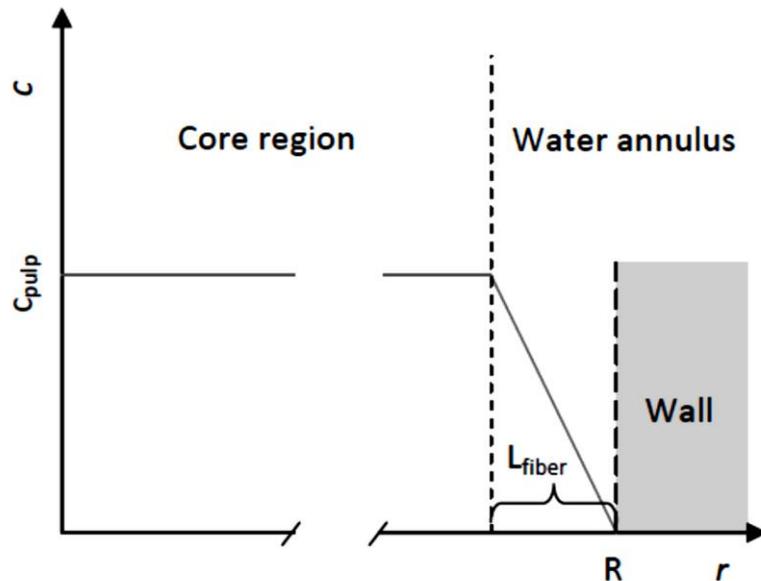
τ_w - stress at the wall

- **Rheological tests** to try obtain information for **low shear rates**.

Bartosik, A. (2010) – "Application of Rheological Models in Prediction of Turbulent Slurry Flow" - Flow Turbulence Combust, 84(2):277-293.



- Development of the "water annulus" model:
 - "water annulus" thickness
 - variation of fibre consistency across -> viscosity



$$c(r) = -c_{pulp} [r - (R - L_{fiber})] / L_{fiber} + c_{pulp}$$

- Apply the CFD model to study the flow of **pine** suspensions.

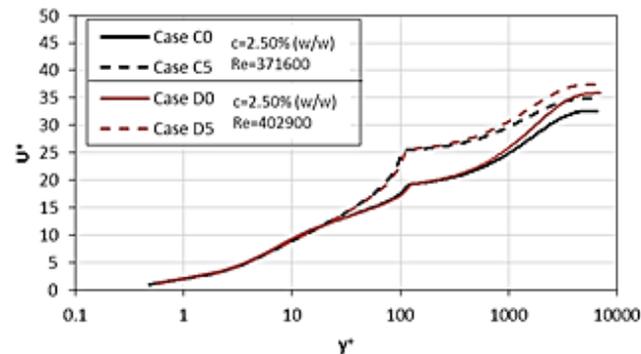
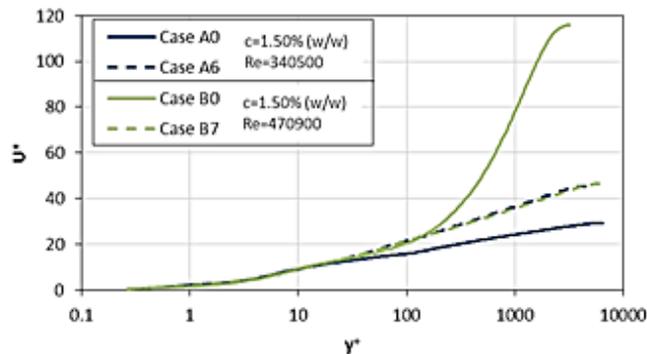


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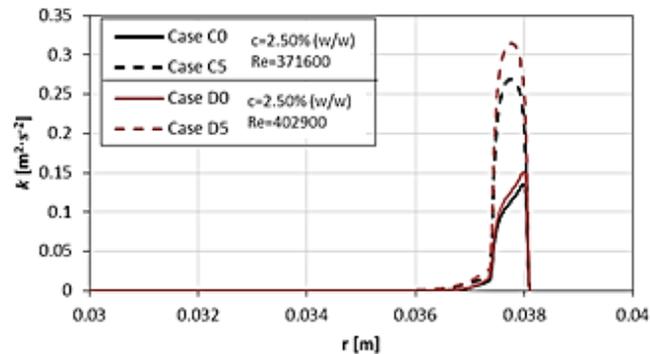
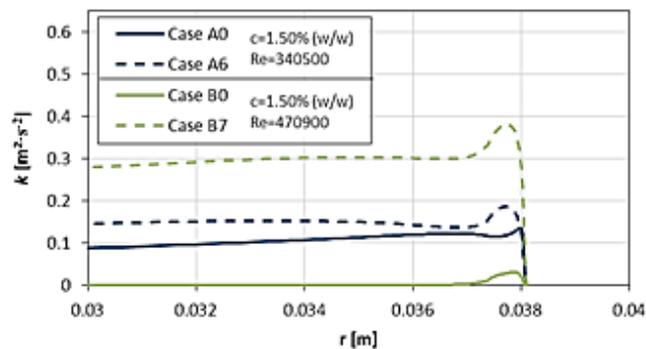
New damping function tested – Bartosik (**AKN** model modified)

Dimensionless velocity



Cases 0 - AKN model without damping function modification

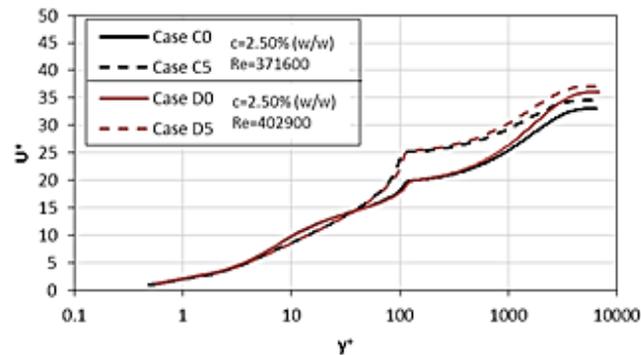
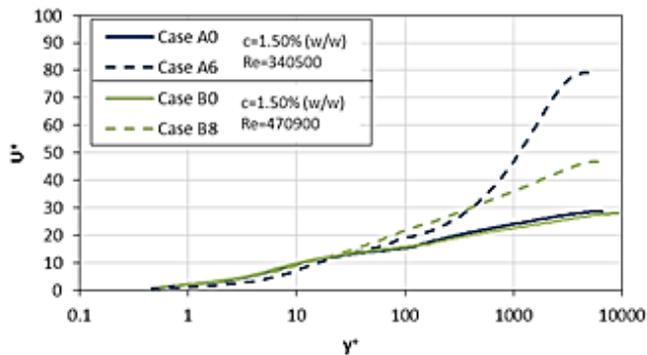
Turbulent kinetic energy





New damping function tested – Bartosik (**CHC** model modified)

Dimensionless velocity



Cases 0 - CHC model without damping function modification

Turbulent kinetic energy

