

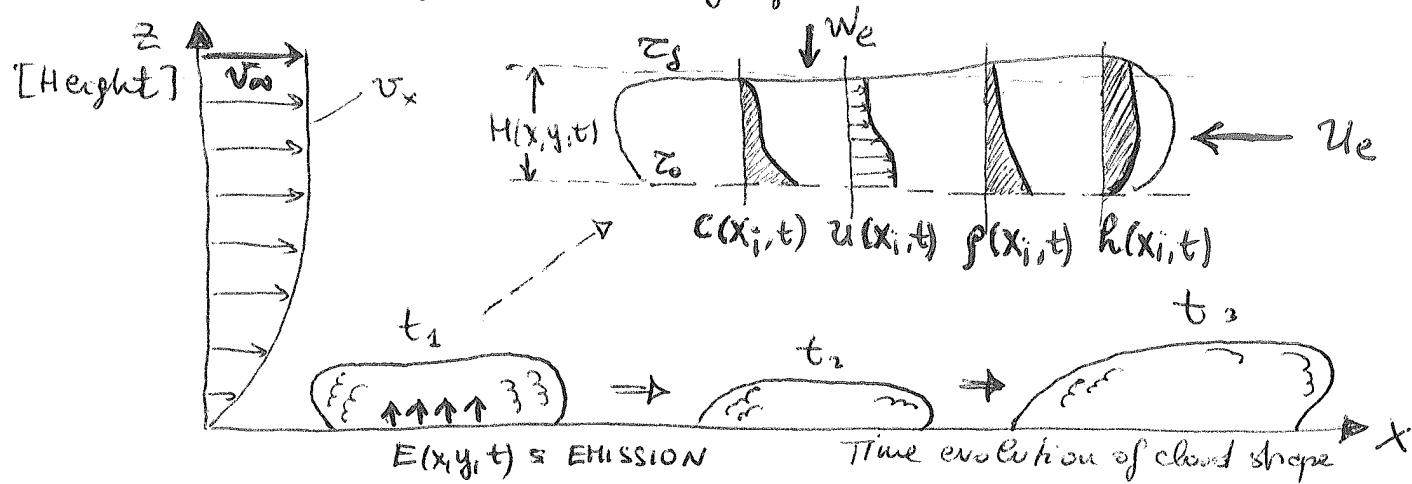
# ATMOSPHERIC DISPERSION

## OF HEAVY GASES

The general physical problem of interest in this section is the dispersion (by mixing with atmospheric air) of a mass of heavy gas that is released during a finite time period into the atmospheric boundary layer.

Different from a neutral gas (which does not alter the behavior of the air, hence the name "passive contaminant"), a heavy gas will spread under the influence of gravity (being denser than the ambient air) and this influence will affect its advection and dispersion by the atmospheric turbulence.

A schematic of the typical development and evolution of a heavy gas "cloud" is the following:



[2]

where :

- $E(x, y, t)$  is the rate at which the heavy gas is issued from the cloud source
- $C(x, y, z, t) = C(x_i, t)$  is the local concentration of the heavy gas
- $\rho(x, y, z, t)$  its density
- $h(x, y, z, t)$  its enthalpy (equivalent to the total heat content within the cloud)
- $u(x, y, z, t)$  the gas velocity profile within the cloud
- $U_e, W_e$  are the entrainment velocities (in the horizontal and vertical directions, respectively), with which atmospheric air is entrained inside the cloud through the front (and side) boundaries -  $U_e$  - and through the top boundary -  $W_e$  - of the cloud.
- $\tau_0, \tau_s$  are the shear stresses generated at the cloud bottom and top surfaces, respectively.

Typically, the phase during which the cloud is formed has a small duration compared to the

L3

time during which the cloud travels to the maximum distance exposed to the threshold value of gas concentration of interest.

The heavy gas cloud is three-dimensional and highly transient. Because of this, a model to predict accurately momentum, mass and energy transfer processes within the cloud (which are of interest because it's these processes that control the evolution of the cloud and its dynamics) is extremely complex and difficult to develop.

Indeed, the cloud evolution is characterized by several distinct stages:

- 1) Emission from a source: the heavy gas is released into the atmosphere, and forms a cloud that has similar vertical and horizontal dimensions in the vicinity of the source (especially in the case of fast release of large amounts of gas). The behaviour of the gas cloud immediately after release is relatively independent of the characteristics of the ambient atmospheric air (e.g. wind field).

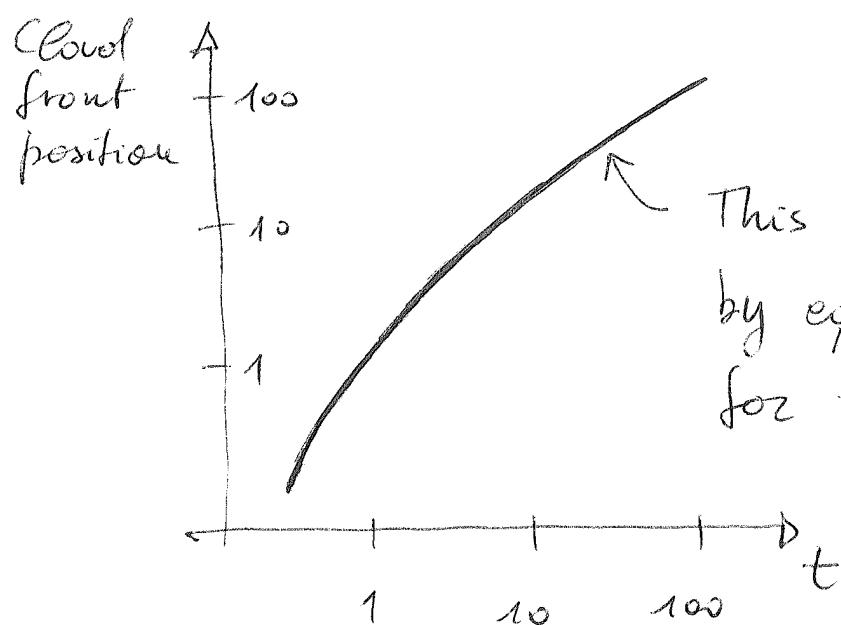
[5]

modelled as a gravity - driven intrusion of the heavy gas into the surrounding air. The transient gravity front that forms can be modelled as a quasi-steady flow in which the buoyancy spreading forces are balanced by the inertial forces. Under such assumptions, the velocity of the front is calculated from the relation:

$$U_f = C_E \cdot \sqrt{g' \cdot H} \quad [1]$$

$$\begin{aligned} g' &= \text{REDUCED} \\ &\text{GRAVITY} \\ &= \frac{P_c - P_a}{P_a} \cdot g \end{aligned}$$

which is obtained from the Bernoulli equation in the case of balance between the potential energy and the kinetic energy of the cloud with negligible viscous dissipation effects.



This curve is well predicted by eq. [1] with  $C_E = 1.16$  for  $t > 20T$ , where  $T = \frac{V^{1/6}}{\sqrt{g'}}$

$T$  is the characteristic time-scale of the cloud release ( $V$  is the cloud volume)

2) Buoyancy-dominated flow regime: close to [4]  
the source, the cloud develops under the  
combined contribution of buoyancy forces,  
inertial forces and ambient air motions.  
In this stage, the cloud "slumps" (to slump =  
to fall or sink suddenly) because it is still  
heavy and spreads over the ground driven  
by gravity. During this process of slumping  
and lateral spreading, the cloud's shape  
resembles that of an expanding vortex ring.  
It has been proven that slumping and lateral  
spreading lead to entrainment of large amounts  
of ambient air (up to ten times the initial  
mass of the cloud): This implies that the density  
ratio between the cloud (not so heavy anymore,  
but the ambient air is reduced by a factor  
of ten, namely that strong dilution takes  
place (dilution factor of ten to one hundred)).

The process of lateral spreading is typically

As far as dilution is concerned, the main observable that needs to be modelled is air entrainment into the heavy gas cloud. In particular the flow rate of entrained air must be modelled. Referring to the schematic of page 1, such flow rate can be expressed as :

$$[2] \quad Q_e = u_e \cdot A_f + w_e \cdot A_t \quad [\text{m}^3/\text{s}]$$

where  $u_e \cdot A_f$  is the horizontal entrainment rate (with  $A_f$  the surface area through which air is entrained horizontally with velocity  $u_e$ ) and  $w_e \cdot A_t$  is the vertical entrainment rate (with  $A_t$  the surface area through which air is entrained vertically with velocity  $w_e$ ).

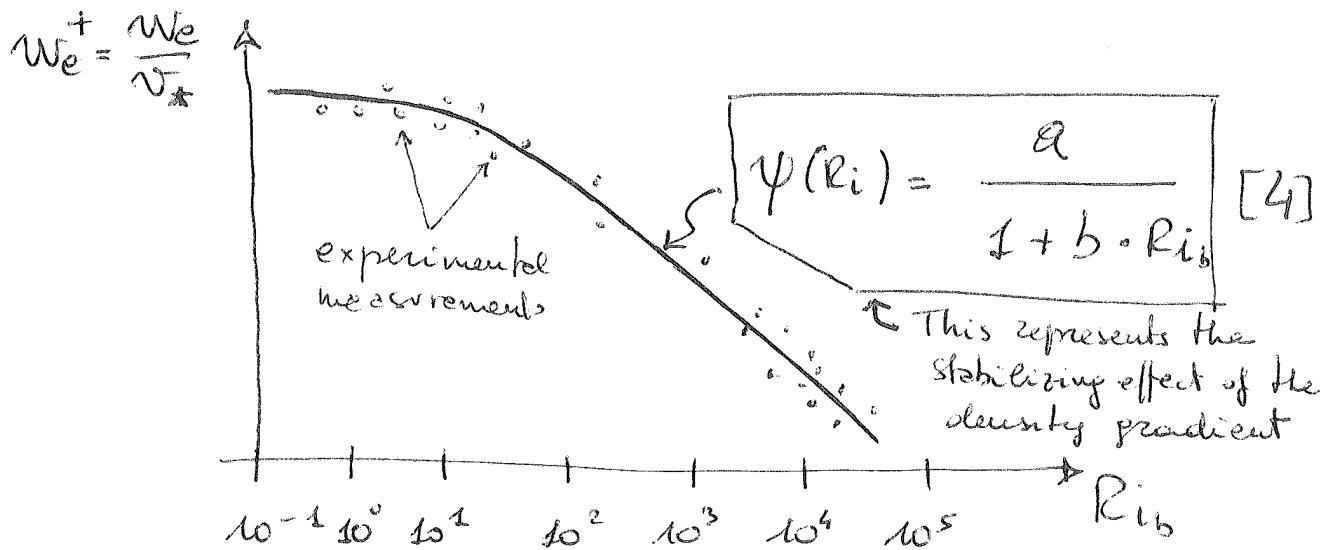
Estimates for  $u_e$  and  $w_e$  are :

$$u_e = C_e \cdot u_f \quad \rightsquigarrow u_e \propto u_f$$

$$[3] \quad w_e = v_* / \psi(R_{ib}) \quad \text{with } v_* = \text{friction velocity}$$

$\psi = \text{function of the bulk Richardson number } R_{ib}$

The correlation of the vertical entrainment velocity with the bulk Richardson number, validated by experimental results, is : L7



where  $a$  and  $b$  are empirical constants.

3) Stably-stratified flow regime: This flow regime represents an intermediate stage of the gas dispersion process, between the buoyancy-dominated flow regime and the latter stages where dispersion becomes passive. This regime is characterized by the persistence of a lateral gravity-driven flow in the cross-wind direction but also by vertical density stratification, which damps turbulent mixing.

The lateral gravity-driven flow can be described

by a stably-stratified cloud embedded in  
the ambient air flow driven by the mean wind  
velocity. Therefore, eq. [1] can still be used  
to compute the front velocity.

As far as vertical mixing is concerned, eqns.  
[3] and [4] can be used: These two equations are  
rather accurate over a wide range of values for  
Rib, encompassing the majority of heavy gas  
dispersion scenarios of practical interest.

Note that air entrainment in the stably-stratified  
flow regime occurs primarily through the top of  
the cloud.

Also note that the suppression of turbulent  
mixing leads to a significant reduction of the  
cloud dilution compared to the buoyancy-domi-  
nated flow regime.

4) Passive turbulent dispersion regime: As the  
dispersion proceeds, the stable stratification de-  
creases until the process can be represented as a

neutrally - buoyant cloud in a neutral or stratified ambient air flow. At this stage, dilution is such that the excess density of the heavy gas cloud has a negligible effect on dispersion and natural levels of turbulence are established again. The gas becomes a passive contaminant, whose dispersion is well described by Gaussian dispersion models.

In this flow regime, the dynamics of the cloud is controlled by ambient turbulence and, therefore, by the mean wind field. The velocity profile in a shear flow against a rough wall boundary (like the one generated by wind blowing near the ground) is determined from :

$$\boxed{\frac{dV_x}{dz} = \frac{1}{K} \cdot \frac{V_*}{z} \cdot \Psi_M \left( \frac{z}{L} \right)} \quad [5]$$

where  $V_x$  is the mean wind velocity,  $K \approx 0.4$  is the Von Karman constant,  $z$  is the vertical height and  $\Psi_M$  is a function of the dimensionless quantity  $\frac{z}{L}$ .

The quantity  $z_L$  is a dimensionless height [10] that provides a measure of the stability of the atmospheric flow at height  $z$ .

$L$  is the OBUKHOV LENGTH, defined by:

$$L \triangleq -\frac{\theta}{g} \cdot \frac{U_*^3}{\bar{w}'\theta'} \cdot \frac{1}{K} \quad [6]$$

where  $\theta$  is the characteristic temperature of the boundary layer within the cloud,  $\bar{w}'\theta'$  is the vertical turbulent heat flux. From eq. [6], the length  $L$  provides a measure of the height at which the production of turbulent kinetic energy by buoyancy is equal to the production of turbulent kinetic energy by the shearing action of the wind (buoyancy production of TKE = shear production of TKE).

Therefore  $L$  expresses the relative importance of shear and buoyancy in the production of energy, and can achieve values of order 1 to tens of meters.  $L$  is positive (negative) for stable (unstable).

stable) stratification, whereas it becomes infinite in the limit of neutral stratification (since  $\overline{w'\theta'} = 0$ ).

Indeed,  $L$  is negative in the daytime (when  $\overline{w'\theta'}$  is usually positive) while  $L$  is positive at night (when  $\overline{w'\theta'}$  is usually negative).

At dawn and dusk,  $\overline{w'\theta'} \rightarrow 0$  and therefore  $L \rightarrow \infty$ .

Going back to eq. [5], when  $L \rightarrow \infty$  then  $\gamma_M = 1$  and one gets:

$$\frac{dN_x}{dz} = \frac{1}{K} \cdot \frac{U_*}{z} \Rightarrow \int_{U_x(z_0)}^{U_x(z)} dN_x = \frac{U_*}{K} \int_{z_0}^z z^{-1} dz$$

with  $z_0$  = roughness height (approximately equal to one-tenth of the height of terrain roughness elements such as trees, crops, canopies, buildings).

Since  $U_x(z_0)$  is assumed to be nearly zero, one gets:

$$\boxed{U_x(z) = \frac{U_*}{K} \ln\left(\frac{z}{z_0}\right)} \Rightarrow U_x^+ = \frac{1}{K} \ln\left(\frac{z}{z_0}\right)$$

Note that  $z_0$  expresses the typical height of terrain elements on which the bulk aerodynamic drag can be exerted and act (below  $z_0$ , no aerodynamic drag is produced). (12)

For the vertical entrainment velocity, one can invoke Reynolds analogy to assume that :

$$\gamma(R_{ib}) \approx \gamma_M \Rightarrow \gamma(R_{ib}) = C \cdot \gamma_M$$

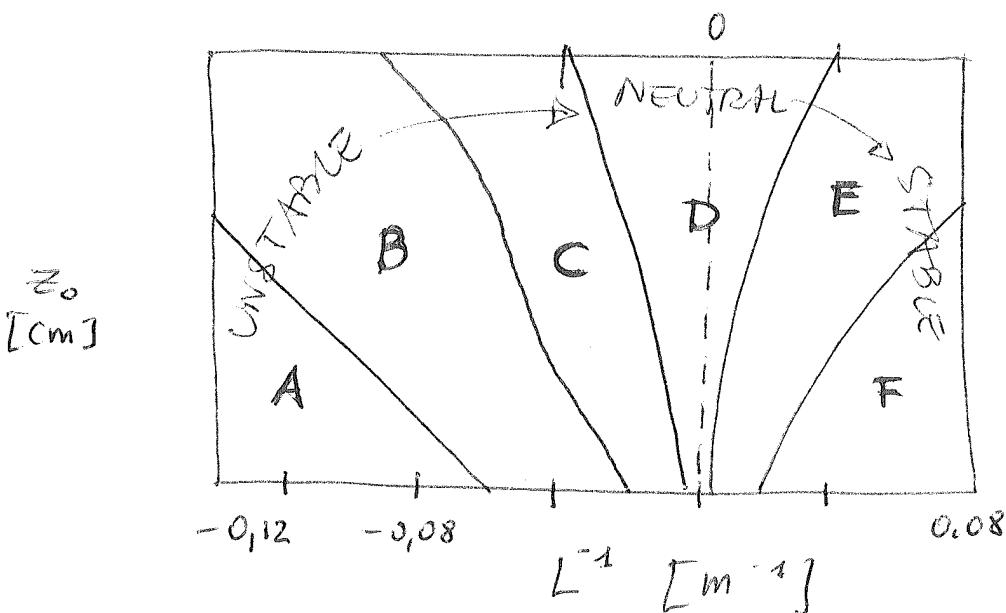
which yields  $W_e = \frac{V_*}{\gamma_M} \cdot \frac{1}{C}$  with  $\frac{1}{C} = K$  (von Karman constant).

Namely :

$$W_e = K \cdot \frac{V_*}{\gamma_M}$$

DIGRESSION : The Obukhov length  $L$  and the roughness height  $z_0$  are used to classify atmospheric stability. The first atmospheric stability classification scheme was proposed by Pasquill in 1961:

- CLASS A : extremely unstable
- B : moderately unstable
- C : slightly unstable
- D : neutral
- E : slightly stable
- F : moderately stable



PASQUILL'S  
STABILITY  
CLASSES

The identification of the stability class is required by the so-called STABILITY-CLASS METHOD to calculate the dispersion parameters  $\delta_y$  and  $\delta_z$ , which represent the cross-wind and vertical standard deviations appearing in the equation of the gas concentration when it is treated as a passive contaminant.

In this latter case, the gas does not alter the density of the ambient air, has no effect on the flow and disperses in such a way that its concentration distribution can be represented, from a statistical point of view, by a Gaussian (bell-shaped) distribution. This is precisely what the gas does in the passive dispersion regime.

Skipping the derivation, it can be shown that the contaminant concentration distribution is given by:

$$C(x, y, z) = \frac{E}{N_x} \cdot g_y(x, y) \cdot g_z(x, z)$$

source emission strength [kg/s]

mean wind velocity

with:

$$g_y(x, y) = \frac{1}{\sqrt{2\pi} \cdot \sigma_y(x)} \cdot \exp \left[ -\frac{1}{2} \left( \frac{y}{\sigma_y(x)} \right)^2 \right]$$

$$g_z(x, z) = \frac{1}{\sqrt{2\pi} \cdot \sigma_z(x)} \cdot \left\{ \exp \left[ -\frac{1}{2} \left( \frac{z - h_s}{\sigma_z(x)} \right)^2 \right] + \exp \left[ -\frac{1}{2} \left( \frac{z + h_s}{\sigma_z(x)} \right)^2 \right] \right\}$$

where  $h_s$  is a distance beneath the ground at which a mirror (fictitious) source of contaminant is ideally placed to model the trapping effect of the ground in case of ground emission.

The model of cloud dispersion that makes use of the above equations to calculate the concentration distribution of the gas inside the cloud can be rendered as follows:

